# The **easing**<sup>\*</sup> Library for PGF

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### 1 Introduction

This library adds easing functions to the PGF mathematical engine.

## 2 Installation

The easing library is a PGF library; it works both with IATEX and with plain TEX. Once the file pgflibraryeasing.code.tex is in a directory searched by TEX, the library can be loaded as follows:

with plain  $T_EX$ :

\input pgf
\usepgflibrary{easing}

with  $LAT_EX$ :

\usepackage{pgf}
\usepgflibrary{easing}

The easing library is compatible with, but does not depend on, the floating point unit library provided by PGF. To use both easing and the FPU, the FPU (or any packages/libraries which use the FPU, such as pgfplots) must be loaded before the easing library.

## 3 Usage

The routines implemented by the easing library are added to PGF's mathematical engine with \pgfmathdeclarefunction, so that they are recognised by by \pgfmathparse and can be used in any expression which is processed by the parser. As a first example, the following code produces plots of the function smoothstep(a, b, x) against the argument x, with one endpoint a = 0 and the other endpoint b ranging through the integers -1 to 3:



(This example also demonstrates the behaviour of the easing functions in some special cases: when the endpoints  $b \leq a$ , and in particular the degenerate case where a = b, in which the library chooses to consider the function that is 1 for all  $x \geq 0$  and 0 otherwise.)

Like all functions declared in this way, the functions implemented by easing are also available as "public" macros, such as \pgfmathsmoothstep:

$S_1(0) = 0.0$ \usepgflibrary{easing}	
$S_1(0.25) = 0.15625$ \foreach\x in{0,0.25,,1}	}{
$S_1(0.5) = 0.5$ \pgfmathsmoothstep{0}{1}	{\x}
$S_1(0.75) = 0.84375$ \$S_1(\x)=\pgfmathresult\$	\par
$S_1(1) = 1.0$ }	
\end	

See Part VIII of the PGF manual for more details on the mathematical engine.

#### 3.1 Naming conventions

For each shape, three functions are declared, all of which take three arguments a, b, and x. Where a < b, all of these function take value 0 whenever  $x \le a$  and 1 whenever  $x \ge b$ . The names of the functions adhere to the following pattern:

- The ease-in form  $\langle shape \rangle easein(a,b,x)$  has easing applied near the endpoint a.
- The *ease-out* form  $\langle shape \rangle$ easeout (a, b, x) has easing applied near the endpoint b. Its graph is that of the ease-in form reflected about both axes.
- The step function form  $\langle shape \rangle$  step(a, b, x) has easing applied near both endpoints. Its graph is that of the ease-in and ease-out forms concatenated then appropriately scaled.



#### 3.2 Specifying parameters

Some of these shapes can be modified by adjusting one or more parameters, which is done through **pgfkeys**: the parameter  $\langle param \rangle$  for functions of shape  $\langle shape \rangle$  is specified by setting the PGF key /easing/ $\langle shape \rangle/\langle param \rangle$ :



Setting a parameter affects the ease-in, step, and ease-out forms of the relevant function at once.

For detailed descriptions of the parameters admitted by each shape, see the following section.

## 4 List of easing function shapes

An exhaustive list follows of all the easing functions implemented by the easing library. For clarity, where mathematical expressions are given for functions, they are written in terms of a parameter t equal to  $\frac{x}{b-a}$ .

#### 4.1 Polynomials

#### 4.1.1 The smooth and smoother shapes

The step function form of the **smooth** shape is a third-order Hermite polynomial interpolation between 0 and 1, so that the first derivate at the endpoints are zero. It is defined  $3t^2 - 2t^3$  for  $0 \le t \le 1$ .

The step function form of the **smoother** shape is a fifth-order Hermite polynomial interpolation between 0 and 1, so that the first and second derivatives at the endpoints are zero. It is defined  $10t^3 - 15t^4 + 6t^5$  for  $0 \le t \le 1$ .



4.1.2 The pow shape and friends (linear, quad, cubic, quart, and quint)

Polynomial easing. The ease-in form is defined as  $t^n$  for  $0 \le t \le 1$ , where the exponent *n* is set with the PGF key /easing/pow/exponent, and should be greater than 0. The parameter defaults to n = 2.4.

When n = 1, the function is linear between 0 and 1. For  $0 < n \le 1$ , the ease-in form has discontinuous derivative at 0.

The shapes linear, quad, cubic, quart, and quint are the same functions as pow with n = 1, ..., 5, respectively. Computations for these shapes are implemented with T<sub>E</sub>X registers, which is a little faster and more accurate than setting the argument then evaluating the equivalent pow function.



4.1.3 The back shape

Anticipatory easing. The ease-in form is defined as  $t^2(1-t)s + t^3$  for  $0 \le t \le 1$ , where the parameter s is set with the PGF key /easing/back/overshoot. The parameter defaults to s = 1.6.

When  $s \leq 0$ , there is no overshoot. When s = 0, the function is equivalent to pow with n = 3.



#### 4.2 Trigonometric and exponential

#### 4.2.1 The sine shape

An easing function that looks like a section of a sinusoid. The ease-out form is defined as  $\sin(\frac{\pi}{2}t)$  for  $0 \le t \le 1$ .

This shape admits no parameters.





An easing function that looks like an exponential function. The ease-in form is defined as  $e^{c(t-1)}$  for  $0 \le t \le 1$ , where the parameter c is set with the PGF key /easing/exp/speed, and should be greater than 0. The parameter defaults to c = 7.2.

Because of the nature of the exponential function, this shape is only approximately continuous at the endpoints a and b. In practice, the discontinuity only becomes noticeable for small c, around  $c \leq 4$ .



#### 4.3 Other

#### 4.3.1 The circ shape

An easing function whose graph is part of an ellipse. This shape admits no parameters.



4.3.2 The elastic shape

Easing function that looks like a damped harmonic oscillator. The ease-out form is defined as  $e^{c}(t-1)\cos(2\pi f(1-t))$ . This shape admits two parameters:

- The frequency f is the number of oscillations between the endpoints. It is set with the PGF key /easing/elastic/frequency, and should be greater than 0. The frequency defaults to f = 3.
- The damping coefficient b affects the speed at which the amplitude decays. It is set with the PGF key /easing/elastic/damping, and should be greater than zero. The damping coefficient defaults to b = 7.2.

The function overshoots the range [0,1] when f > 0.5. For  $0 < f \leq 1$ , this function becomes a family of anticipatory easing curves that look slightly different from the **back** shape but are more expensive to compute.



### 5 Implementation

\ifeasing@withfpu This library uses TFX registers and PGF's mathematical engine for computations. \easing@divide It is possible that the user is loading this library together with the floating point unit library. We save the basic routines from pgfmath, so that when this happens, the FPU doesn't break everything when it does a switcharoo with the pgfmath macros. 1 \newif\ifeasing@withfpu 2 \expandafter\ifx\csname pgflibraryfpuifactive\endcsname\relax 3 \easing@withfpufalse 4 \else 5 \easing@withfputrue 6 \fi 7 \ifeasing@withfpu 8 \let\easing@cos\pgfmath@basic@cos@ 9 \let\easing@divide\pgfmath@basic@divide@ 10 \let\easing@exp\pgfmath@basic@exp@ 11 \let\easing@ln\pgfmath@basic@ln@ 12 \let\easing@sqrt\pgfmath@basic@sqrt@ 13 \else 14 \let\easing@cos\pgfmathcos@ 15 \let\easing@divide\pgfmathdivide@ 16 \let\easing@exp\pgfmathexp@ 17 \let\easing@ln\pgfmathln@ 18 \let\easing@sqrt\pgfmathsqrt@

In absence of the FPU, the next section of code defines \easing@linearstep, which expects as arguments plain numbers (i.e. things that can be assigned to dimension registers). The net effect of \easing@linearstep{#1}{#2}{#3} is to set \pgfmathresult to  $\frac{\#3-\#1}{#2-\#1}$ , clamped to between 0 and 1.

If the FPU is loaded, \easing@linearstep is instead named \easing@linearstep@fixed, and we additionally define \easing@linearstep@float, which expects FPUformat floats as arguments. We do not format the output as a float since the FPU is smart enough to do that conversion quietly on its own.

The **\easing@linearstep** routine is the first step in the definition of all other routines that compute easing functions.

- 20 \def\easing@linearstep@ne#1{%
- 21 \begingroup
- 22 \pgf@x#1pt
- 23 \ifdim1pt<\pgf@x\pgf@x 1pt\fi
- 24 \ifdimOpt>\pgf@x\pgf@x Opt\fi
- 25 \pgfmathreturn\pgf@x
- 26 \endgroup

```
27 }%
```

19 \fi

```
\advance\pgf@xa-\pgf@xc
37
              \advance\pgf@xb-\pgf@xc
38
              \easing@divide{\pgfmath@tonumber\pgf@xa}{\pgfmath@tonumber\pgf@xb}%
39
              \easing@linearstep@ne\pgfmathresult
40
41
              \fi
              \pgfmathsmuggle\pgfmathresult
42
              \endgroup
43
44 }%
45 \ ifeasing@withfpu
46 \def\easing@linearstep@float#1#2#3{%
47
             \begingroup
              \pgfmathfloatsubtract{#3}{#1}%
48
              \edef\pgf@tempa{\pgfmathresult}%
49
              \pgfmathfloatsubtract{#2}{#1}%
50
              \edef\pgf@tempb{\pgfmathresult}%
51
52
              \pgfmathfloatifflags{\pgf@tempb}{0}{%
53
                     \pgfmathfloatifflags{\pgf@tempa}{-}{%
                            \edef\pgfmathresult{0}%
54
55
                    }{%
                           \ensuremath{\ensuremath{\mathsf{l}}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\xspace_{1}\x
56
                    }%
57
             }{%
58
59
                     \pgfmathfloatdivide\pgf@tempa\pgf@tempb
60
                     \pgfmathfloattofixed{\pgfmathresult}%
                     \easing@linearstep@ne\pgfmathresult
61
             }%
62
              \pgfmathsmuggle\pgfmathresult
63
              \endgroup
64
65 }%
66 \def\easing@linearstep#1#2#3{%
             \pgflibraryfpuifactive{%
67
68
                     \easing@linearstep@float{#1}{#2}{#3}}{%
                     \easing@linearstep@fixed{#1}{#2}{#3}}%
69
70 }%
71 \fi
```

28 \expandafter\def

\begingroup

\pgf@xa#3pt

\pgf@xb#2pt

\pgf@xc#1pt

\else

\ifdim\pgf@xb=\pgf@xc

30

 $31 \\ 32$ 

33

34

35

36

\easing@linearstep@easein@ne
\easing@linearstep@easeout@ne

The linear ease-in and ease-out functions are identical to the linear step function. We define the respective macros so as not to surprise the user with their absence.

29 \csname easing@linearstep\ifeasing@withfpu @fixed\fi\endcsname#1#2#3{%

\edef\pgfmathresult{\ifdim\pgf@xa>\pgf@xb 1\else 0\fi}%

72 \let\easing@lineareasein\easing@linearstep

```
73 \pgfmathdeclarefunction{lineareasein}{3}{%
```

```
74 \easing@lineareasein{#1}{#2}{#3}}%
75 \let\easing@lineareaseout\easing@linearstep
76 \pgfmathdeclarefunction{lineareaseout}{3}{%
```

77  $\easing@lineareasein{#1}{#2}{#3}}%$ 

\easing@derive@easein@nefromstep@ne
 \easing@derive@easeout@nefromstep@ne
 \easing@derive@step@nefromeasein@ne
 \easing@derive@easeout@nefromeasein@ne

The pattern in general is that, for each shape, we define the one-parameter version of the step, ease-in, and ease-out routines interpolating between values 0 at 1 at the ends of the unit interval. Then by composing with **\easing@linearstep**, we obtain the three-parameter versions that allow the user to specify the begin and end points of the interpolation.

Most of the time it suffices to define just one of the three one-parameter versions of a shape to be able to infer the form of all three. This is done with the \easing@derive-from- macros.

```
78 \def\easing@derive@easein@nefromstep@ne#1{%
```

- 79 \expandafter\def\csname easing@#1easein@ne\endcsname##1{%
- 80 \begingroup
- 81 \pgf@x##1 pt
- 82 \divide\pgf@x 2
- 83 \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
- 84 \pgf@x\pgfmathresult pt
- 85 \multiply\pgf@x 2
- 86 \pgfmathreturn\pgf@x
- 87 \endgroup
- 88 **}%**
- 89 }%
- 90 \def\easing@derive@easeout@nefromstep@ne#1{%
- 91 \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
- 92 \begingroup
- 93 \pgf@x##1 pt
- 94 \divide\pgf@x 2
- 95 \advance\pgf@x 0.5pt
- 96 \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
- 97 \pgf@x\pgfmathresult pt
- 98 \multiply\pgf@x 2
- 99 \advance\pgf@x -1pt
- 100 \pgfmathreturn\pgf@x
- 101 \endgroup
- 102 }%
- 103 }%
- 104 \def\easing@derive@step@nefromeasein@ne#1{%
- 105 \expandafter\def\csname easing@#1step@ne\endcsname##1{%
  - 106 \begingroup
  - 107 \pgf@x##1 pt
  - 108 \multiply\pgf@x 2
  - 109 \ifdim\pgf@x<1pt
  - 110 \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
  - 111 \pgf@x\pgfmathresult pt
  - 112 \divide\pgf@x 2

```
\else
                        113
                                \multiply\pgf@x -1
                        114
                                \advance\pgf@x 2pt
                        115
                                \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
                        116
                        117
                                \pgf@x\pgfmathresult pt
                        118
                                \divide\pgf@x 2
                        119
                                \multiply\pgf@x -1
                                \advance\pgf@x 1pt
                        120
                                \fi
                        121
                                \pgfmathreturn\pgf@x
                        122
                        123
                                \endgroup
                             }%
                        124
                        125 }%
                        126 \def\easing@derive@easeout@nefromeasein@ne#1{%
                              \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
                        127
                                \begingroup
                        128
                                \pgf@x##1pt
                        129
                                \multiply\pgf@x -1
                        130
                        131
                                \advance\pgf@x 1pt
                        132
                                \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
                        133
                                \pgf@x\pgfmathresult pt
                                \multiply\pgf@x -1
                        134
                                \advance\pgf@x 1pt
                        135
                                \pgfmathreturn\pgf@x
                        136
                        137
                                \endgroup
                             }%
                        138
                        139 }%
                         The three-parameter versions of each routine is installed into the mathematical
\easing@pgfmathinstall
                         engine, so that they are available in \pgfmathparse.
                        140 \def\easing@pgfmathinstall#1{%
                              \pgfmathdeclarefunction{#1step}{3}{%
                        141
                                \easing@linearstep{##1}{##2}{##3}%
                        142
                                \csname easing@#1step@ne\endcsname\pgfmathresult
                        143
```

```
144 }%
```

```
145 \pgfmathdeclarefunction{#1easein}{3}{%
146 \easing@linearstep{##1}{##2}{##3}%
```

```
    147 \csname easing@#1easein@ne\endcsname\pgfmathresult
```

```
147
148 }%
```

```
149 \pgfmathdeclarefunction{#1easeout}{3}{%
```

```
150 \easing@linearstep{##1}{##2}{##3}%
```

```
151 \csname easing@#1easeout@ne\endcsname\pgfmathresult
```

```
152 }%
153 }%
```

\easing@smoothstep@ne
\easing@smootheasein@ne
\easing@smootheaseout@ne

```
e The smooth shape.
```

154 \def\easing@smoothstep@ne#1{%
155 \begingroup

\pgf@x#1pt 156\edef\pgf@temp{\pgfmath@tonumber\pgf@x}% 157 \multiply\pgf@x-2 158 \advance\pgf@x 3pt 159160\pgf@x\pgf@temp\pgf@x 161\pgf@x\pgf@temp\pgf@x 162\pgfmathreturn\pgf@x 163\endgroup 164 }% 165 \easing@derive@easein@nefromstep@ne{smooth}% 166 \easing@derive@easeout@nefromstep@ne{smooth}% 167 \easing@pgfmathinstall{smooth}% \easing@smootherstep@ne The smoother shape. \easing@smoothereasein@ne 168 \def\easing@smootherstep@ne#1{% \easing@smoothereaseout@ne \begingroup 169\pgf@x#1pt 170\edef\pgf@temp{\pgfmath@tonumber\pgf@x}% 171\multiply\pgf@x 6 172\advance\pgf@x -15pt 173174\pgf@x\pgf@temp\pgf@x 175\advance\pgf@x 10pt 176\pgf@x\pgf@temp\pgf@x 177\pgf@x\pgf@temp\pgf@x \pgf@x\pgf@temp\pgf@x 178 \pgfmathreturn\pgf@x 179 \endgroup 180 181 }% 182 \easing@derive@easein@nefromstep@ne{smoother}% 183 \easing@derive@easeout@nefromstep@ne{smoother}% 184 \easing@pgfmathinstall{smoother}% The pow shape. \easing@powstep@ne \easing@poweasein@ne Because of some wonkiness in the FPU, \pgfmath@pow@basic@ actually doesn't \easing@poweaseout@ne work. Instead of invoking the pow function, we compute  $t^n$  approximately by computing  $e^{n \ln t}$  using ln and exp instead (which is what pgfmath does anyway when the exponent is not an integer.) 185 \pgfkeys{/easing/.is family}% 186 \pgfkeys{easing, pow/exponent/.estore in=\easing@param@pow@exponent, 187pow/exponent/.default=2.4, 188pow/exponent}% 189 190 \def\easing@poweasein@ne#1{% \begingroup 191 \pgf@x#1pt 192193\ifdim\pgf@x=0pt

194  $\ensuremath{0}\$ 

```
\else
                    195
                          \easing@ln{#1}%
                    196
                          \pgf@x\pgfmathresult pt
                    197
                          \pgf@x\easing@param@pow@exponent\pgf@x
                    198
                          \easing@exp{\pgfmath@tonumber\pgf@x}%
                    199
                    200
                          \fi
                    201
                          \pgfmathsmuggle\pgfmathresult
                    202
                          \endgroup
                    203 }%
                    204 \easing@derive@easeout@nefromeasein@ne{pow}%
                    205 \easing@derive@step@nefromeasein@ne{pow}%
                    206 \easing@pgfmathinstall{pow}%
\easing@quadstep@ne
                     The quad-, cubic-, quart-, and quint- routines have explicit definitions.
                    207 \def\easing@quadeasein@ne#1{%
                          \begingroup
                    208
                     209
                          \pgf@x#1pt
                          \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                    210
                    211
                          \pgf@x\pgf@temp\pgf@x
                          \pgfmathreturn\pgf@x
                          \endgroup
```

```
\easing@quadeasein@ne
\easing@quadeaseout@ne
  \easing@cubicstep@ne
\easing@cubiceasein@ne
\easing@cubiceaseout@ne
  \easing@quartstep@ne 212
\easing@quarteasein@ne 213
\easing@quarteaseout@ne 214 }%
```

```
\easing@quintstep@ne 215 \easing@derive@step@nefromeasein@ne{quad}%
 \easing@quinteasein@ne 216 \easing@derive@easeout@nefromeasein@ne{quad}%
\label{eq:lassing} $$ easing Qquintease out Qne $217 easing Qpgfmathinstall {quad} $$
                          218 🖌
                          219 \def\easing@cubiceasein@ne#1{%
                          220
                               \begingroup
                          221
                               \pgf@x#1pt
                               \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                          222
                          223
                               \pgf@x\pgf@temp\pgf@x
                               \pgf@x\pgf@temp\pgf@x
                          224
                          225
                               \pgfmathreturn\pgf@x
                          226
                               \endgroup
                          227 }%
                          228 \easing@derive@step@nefromeasein@ne{cubic}%
                          229 \easing@derive@easeout@nefromeasein@ne{cubic}%
                          230 \easing@pgfmathinstall{cubic}%
                          231 %
                          232 \def\easing@quarteasein@ne#1{%
                          233
                               \begingroup
                          234
                               \pgf@x#1pt
                               \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                          235
                               \pgf@x\pgf@temp\pgf@x
                          236
                               \pgf@x\pgf@temp\pgf@x
                          237
                               \pgf@x\pgf@temp\pgf@x
                          238
                               \pgfmathreturn\pgf@x
                          239
                          240
                               \endgroup
                          241 }%
```

```
242 \easing@derive@step@nefromeasein@ne{quart}%
                        243 \easing@derive@easeout@nefromeasein@ne{quart}%
                        244 \easing@pgfmathinstall{quart}%
                        245 %
                        246 \def\easing@quinteasein@ne#1{%
                        247
                             \begingroup
                        248
                             \pgf@x#1pt
                             \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                        249
                             \pgf@x\pgf@temp\pgf@x
                        250
                             \pgf@x\pgf@temp\pgf@x
                        251
                             \pgf@x\pgf@temp\pgf@x
                        252
                        253
                             \pgf@x\pgf@temp\pgf@x
                             \pgfmathreturn\pgf@x
                        254
                        255
                             \endgroup
                        256 }%
                        257 \easing@derive@step@nefromeasein@ne{quint}\%
                        258 \easing@derive@easeout@nefromeasein@ne{quint}\%
                        259 \easing@pgfmathinstall{quint}%
   \easing@backstep@ne
                        The back shape.
 \easing@backeasein@ne
                        260 \pgfkeys{easing,
\easing@backeaseout@ne
                             back/overshoot/.estore in=\easing@param@back@overshoot,
                        261
                        262
                             back/overshoot/.default=1.6,
                             back/overshoot}%
                        263
                        264 \def\easing@backeasein@ne#1{%
                             \begingroup
                        265
                             \pgf@x#1pt
                        266
                             \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                        267
                             \advance\pgf@x -1pt
                        268
                             \pgf@x\easing@param@back@overshoot\pgf@x
                        269
                        270
                             \advance\pgf@x\pgf@temp pt
                             \pgf@x\pgf@temp\pgf@x
                        271
                        272
                             \pgf@x\pgf@temp\pgf@x
                             \pgfmathreturn\pgf@x
                        273
                        274
                             \endgroup
                        275 }%
                        276 \easing@derive@step@nefromeasein@ne{back}%
                        277 \easing@derive@easeout@nefromeasein@ne{back}\%
                        278 \ensuremath{\ensuremath{\mathsf{lack}}}\
   \easing@sinestep@ne
                        The sine shape.
 \easing@sineeasein@ne
                         We write down both the easein and step forms of this, since they are simple
\easing@sineeaseout@ne
                         compared to what would have been obtained by \easing@derive-.
                        279 \def\easing@sineeasein@ne#1{%
```

- 280 \begingroup
- 281 \pgf@x**#1**pt
- 282 \multiply\pgf@x 90

	283 \easing@cos{\pgfmath@tonumber\pgf@x}%
	284 \pgf@x\pgfmathresult pt
	285 \multiply\pgf@x -1
	286 \advance\pgf@x 1pt
	287 \pgfmathreturn\pgf@x
	288 \endgroup
	289 1%
	200 \def\easing@sinesten@ne#1{%
	201 (beging top)
	292 \pgies#ipt
	293 (multiply)pgiex 180
	294 (easing@cost\pgimatn@tonumber\pgiwx}%
	295 \pgf@x\pgImathresult pt
	296 \divide\pgf@x 2
	297 \multiply\pgf@x -1
	298 \advance\pgf@x 0.5pt
	299 \pgfmathreturn\pgf@x
	300 \endgroup
	301 }%
	302 \easing@derive@easeout@nefromeasein@ne{sine}%
	303 \easing@pgfmathinstall{sine}%
\easing@expstep@ne	The exp shape
\oogingeonpoopeno	
(easing@expeaseinene	304 easing.
\easing@expeaseout@ne	305 exp/speed/.estore in=\easing@param@exponent@speed.
	306 exp/speed/ default=7 2
	and exp(speed)
	308 \def\easingderneaseindna#1{%
	200 Vestingespeasements (%
	Sid \pgieseript
	311 \advance\pgr@x -1pt
	312 \pgr@x\easing@param@exponent@speed\pgr@x
	313 \easing@exp{\pgimath@tonumber\pgi@x}%
	314 \pgfmathsmuggle\pgfmathresult
	315 Vendgroup
	316 5%
	317 \easing@derive@step@nefromeasein@ne{exp}%
	318 \easing@derive@easeout@nefromeasein@ne{exp}%
	319 \easing@pgfmathinstall{exp}%
\easing@circstep@ne	The circ shape.
\easing@circeasein@ne	
\easing@circeaseout@ne	320 \def\easing@circeasein@ne#1{%
/entreentrelle	321 \begingroup
	322 \pgf@x#1pt
	323 \advance\pgf@x -1pt
	324 \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
	325 \pgf@x\pgf@temp\pgf@x
	326 \multiply\pgf@x -1
	1 0 10

```
327
                                                                            \advance\pgf@x 1pt
                                                               328
                                                                            \easing@sqrt{\pgfmath@tonumber\pgf@x}%
                                                                            \pgfmathsmuggle\pgfmathresult
                                                               329
                                                                            \endgroup
                                                               330
                                                               331 }%
                                                               332 \easing@derive@step@nefromeasein@ne{circ}%
                                                               333 \easing@derive@easeout@nefromeasein@ne{circ}%
                                                               334 \ensuremath{\ensuremath{\mathsf{linstall}}\xspace{\ensuremath{\mathsf{circ}}\xspace{\ensuremath{\mathsf{k}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\m}}\xspace{\ensuremath{\m}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\m}\xspace{\ensuremath{\mathsf{m}}\xspace{\ensuremath{\m}}\xspace{\ensuremath{\m}\xspace{\ensuremath{\m}}\xspace{\ensuremath{\m}}\xspace{\ensuremath{\m}\xspace{\m}\xspace{\ensuremath{\m}\xspace{\m}\xspace{\ensuremath{\m}\xspace{\m}\xspace{\m}\m}\xspace{\ensuremath{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\xspace{\m}\m}\xspace{\m}\m}\m}\xspace{\m}\m}\m}\m}\xspace{\m}\m}\m}\m}\m}\m}\m}\m)
                                                                 The elastic shape.
       \easing@elasticstep@ne
  \easing@elasticeasein@ne
                                                               335 \pgfkeys{easing,
\easing@elasticeaseout@ne
                                                                            elastic/frequency/.estore in=\easing@param@elastic@frequency,
                                                               336
                                                                            elastic/damping/.estore in=\easing@param@elastic@damping,
                                                               337
                                                                            elastic/frequency/.default=3,
                                                               338
                                                                            elastic/damping/.default=7.2,
                                                               339
                                                                            elastic/frequency, elastic/damping}%
                                                               340
                                                               341 \def\easing@elasticeasein@ne#1{%
                                                                            \begingroup
                                                               342
                                                                            \pgf@xa#1pt
                                                               343
                                                                            \advance\pgf@xa -1pt
                                                               344
                                                                            \pgf@xb-\pgf@xa
                                                               345
                                                               346
                                                                            \pgf@xa\easing@param@elastic@damping\pgf@xa
                                                               347
                                                                             \easing@exp{\pgfmath@tonumber\pgf@xa}%
                                                                            \pgf@xa\pgfmathresult pt
                                                               348
                                                                            \pgf@xb 360\pgf@xb
                                                               349
                                                                            \pgf@xb\easing@param@elastic@frequency\pgf@xb
                                                               350
                                                                            \easing@cos{\pgfmath@tonumber\pgf@xb}%
                                                               351
                                                                            \pgf@xa\pgfmathresult\pgf@xa
                                                               352
                                                               353
                                                                            \pgfmathreturn\pgf@xa
                                                                            \endgroup
                                                               354
                                                               355 }%
                                                               356 \easing@derive@step@nefromeasein@ne{elastic}%
                                                               357 \easing@derive@easeout@nefromeasein@ne{elastic}%
```

```
358 \easing@pgfmathinstall{elastic}\%
```

## **Change History**

```
0.1
```

General: Initial version ..... 1